

# Fluids and Pressure

**Density**  $\rho = \text{mass/volume}$  [ $\text{kg/m}^3$ ]

- Specific gravity  $SG = \rho_{\text{object}} / \rho_{\text{water}}$  If  $SG > 1$  sinks, if  $SG < 1$  floats
- Specific gravity  $SG =$  fraction of floating object below the water
- $\rho_{\text{water}} = 1000 \text{ kg/m}^3$

**Pressure**  $P = \text{Force/Area}$  [ $\text{N/m}^2 = \text{Pascals}$ ]

- $P_{\text{atm}} = 1.01 \times 10^5 \text{ Pa}$
- A small force can exert a huge pressure if area of contact is small (e.g. pushing tack into wall)

$P_{\text{absolute}} = P_o + \rho gh$                        $P_{\text{gauge}} = \rho gh$

- $P_o$  is the pressure above the fluid, which is usually  $P_{\text{atm}} = 1.01 \times 10^5 \text{ Pa}$
- $P_{\text{gauge}}$  measures the difference between the fluid pressure and atmospheric pressure
- $P_{\text{gauge}}$  is what you measure when you check your tires

**Volume flow rate** = (Area)(speed) [ $\text{m}^3/\text{sec}$ ]

$A_1 v_1 = A_2 v_2$                       ( or  $Av = \text{constant}$  )

- Note: This is true for liquids, not gases, because liquids are incompressible

## **Buoyancy**

- **Archimedes principle:** The Buoyant force equals the weight of the fluid displaced

$F_{\text{buoyancy}} = \rho_{\text{fluid}} V_{\text{fluid displaced}} g$

- The  $V_{\text{fluid displaced}}$  is not always the volume of the object! (unless it is completely submerged)
- $F_{\text{buoyancy}} = \text{Weight in air} - \text{Weight in water}$  (for objects that don't float)

## **Bernoulli's Equation**

$P_1 + \frac{1}{2}\rho v_1^2 + \rho gh_1 = P_2 + \frac{1}{2}\rho v_2^2 + \rho gh_2$

Note: If the height does not change significantly, Bernoulli's eqn says,

$P_1 + \frac{1}{2}\rho v_1^2 = P_2 + \frac{1}{2}\rho v_2^2$                       ( or  $P + \frac{1}{2}\rho v^2 = \text{constant}$  )

- **Bernoulli's principle:** If the speed of a fluid increases, the pressure of the fluid decreases
- e.g. Blowing air over paper decreases pressure on top, and the paper rises

# Thermal Physics

## Thermal expansion

$$\Delta L = \alpha L_0 \Delta T \text{ [m]}$$

- Note:  $\Delta T$  can be in  $^{\circ}\text{C}$  or K, but if you have an equation with just T it must be in K
- Almost all objects expand when heated (note: holes in heated objects also expand)

## Thermal conduction

$$Q/\text{time} = kA \Delta T/L \text{ [J/sec or Watts]}$$

- Heat Q passes through a material of area A, thickness L, and thermal conductivity k
- **Conduction** is when heat flows through an object, **convection** is when currents of hot fluid flow to colder regions, and **radiation** is when energy is transferred by EM waves

$$PV = nRT$$

(n=moles, T in K, R = 8.31 Pa m<sup>3</sup> /mol K, R = 0.082 atm L /mol K)

$$PV = Nk_B T$$

(N = # molecules, T in K, P in Pa, V in m<sup>3</sup>, k<sub>B</sub> = 1.38 x 10<sup>-23</sup> J/K)

$$Q_{\text{gained}} = Q_{\text{lost}}$$

(note: Heat is measured in Joules)

$$Q = mc \Delta T$$

(use when object is changing temperature)

$$Q = mL$$

(use when object is changing phase, e.g. solid to liquid or liquid to gas)

- use **heat of fusion** for (solid <-> liquid) use **heat of vaporization** for (liquid <-> gas)

$$V_{\text{rms}} = [3k_B T / M_{\text{molecule}}]^{1/2}$$

(root-mean-square speed of molecule in an ideal gas)

## Laws of thermodynamics

$$\text{First Law: } \Delta U = Q_{\text{heat flows into gas}} + W_{\text{work done on gas}}$$

- Internal energy (U) increases if heat Q flows into a gas, or work W is done on a gas
- If internal energy of a gas increases, then T increases.
- For Monatomic Ideal Gas you can use the equation  $\Delta U = 3/2 \Delta(PV)$

## **Second Law: Entropy of universe is always increasing**

- heat never flows spontaneously from cold to hot
- no heat engine can have an efficiency of 1

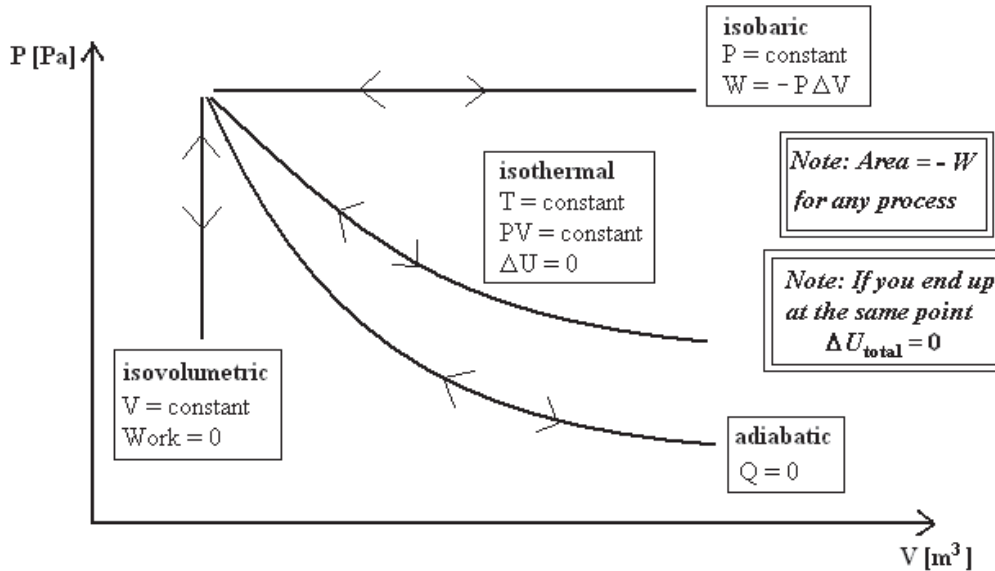
$$\text{efficiency} = W/Q_H = 1 - Q_C/Q_H \text{ (} Q_C \text{ is waste heat created by heat engine)}$$

- The most efficient engine (Carnot engine) has efficiency of  $e = 1 - T_C/T_H$

## **Change in entropy $\Delta S = Q/T$**

- if heat flows into an object, that object's entropy increases (and vice versa)

# Common thermal processes



## Important things to know about PV diagrams

moving to right is expansion  
(- work is done on gas)

moving to left is compression  
(+ work is done on gas)

Work done on gas  
= - Work done by gas

Moving to larger PV (up and right)  
means  $\Delta U$  is +  
(and since  $W$  is -,  $Q$  must be +)

Moving to lower PV (down and left)  
means  $\Delta U$  is -  
(and since  $W$  is +,  $Q$  must be -)

### Example 1

An ice cube at  $-35^\circ\text{C}$  is dropped into a 100g aluminum container that holds 300g of water at  $50^\circ\text{C}$ . If the equilibrium temperature reached is  $20^\circ\text{C}$ , what was the mass of the ice cube?

$$c_{\text{water}} = 4186 \text{ J/kg }^\circ\text{C}$$

$$c_{\text{ice}} = 2100 \text{ J/kg }^\circ\text{C}$$

$$c_{\text{aluminum}} = 900 \text{ J/kg }^\circ\text{C}$$

$$L_{\text{fusion}} = 330,000 \text{ J/kg}$$

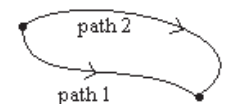
$$Q_{\text{gained}} = Q_{\text{lost}} \quad (\text{Note: ice cube gains heat, but water and aluminum lose heat})$$

$$m(2100)[0^\circ\text{C} - (-35^\circ\text{C})] + m(330,000) + m(4186)(20^\circ\text{C} - 0) = (0.1\text{kg})(900)(50^\circ\text{C} - 20^\circ\text{C}) + (0.3\text{kg})(4186)(50^\circ\text{C} - 20^\circ\text{C})$$

$$m(487220) = 40374$$

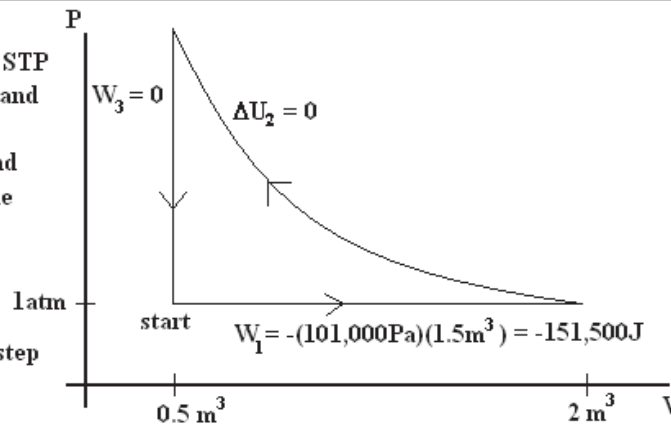
$$m = 0.083 \text{ kg}$$

If two paths start at the same point, and end up at the same point,  $\Delta U$  will be the same for both paths ( $Q$  and  $W$  will not)



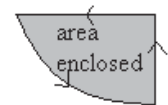
### Example 2

A  $0.5 \text{ m}^3$  sample of an ideal gas starts at STP and expands to  $2 \text{ m}^3$  at constant pressure and absorbs 200,000J of heat. Then the gas is compressed isothermally back to  $0.5 \text{ m}^3$  and the gas does 320,000J of work. Finally the gas is cooled at constant volume back to 1atm.



Draw the process on a PV diagram and determine the  $\Delta U$ ,  $Q$  and  $W$  for each step and the whole process.

The total area enclosed by a closed path will tell you the total work done (could be + or -)



For an enclosed area the total work done on gas is + if top line goes to the left (as seen in the above diagram)

path 1	path 2	path 3	total path
$W = -151,500 \text{ J}$	$W = 320,000 \text{ J}$	$W = 0$	$W = 168,500 \text{ J}$
$Q = +200,000 \text{ J}$	$Q = -320,000$	$Q = -48,500 \text{ J}$	$Q = -168,500 \text{ J}$
$\Delta U = +48,500 \text{ J}$	$\Delta U = 0$	$\Delta U = -48,500 \text{ J}$	$\Delta U = 0$

# Electric Forces, Fields, Energy & Voltage

**F<sub>e</sub>** is electric force [Newtons]

+ charges feel force in same dir of the electric field (E), - charges feel force in opp. dir of electric field (E)

**E** is electric field [N/Coulomb or Volts/meter]

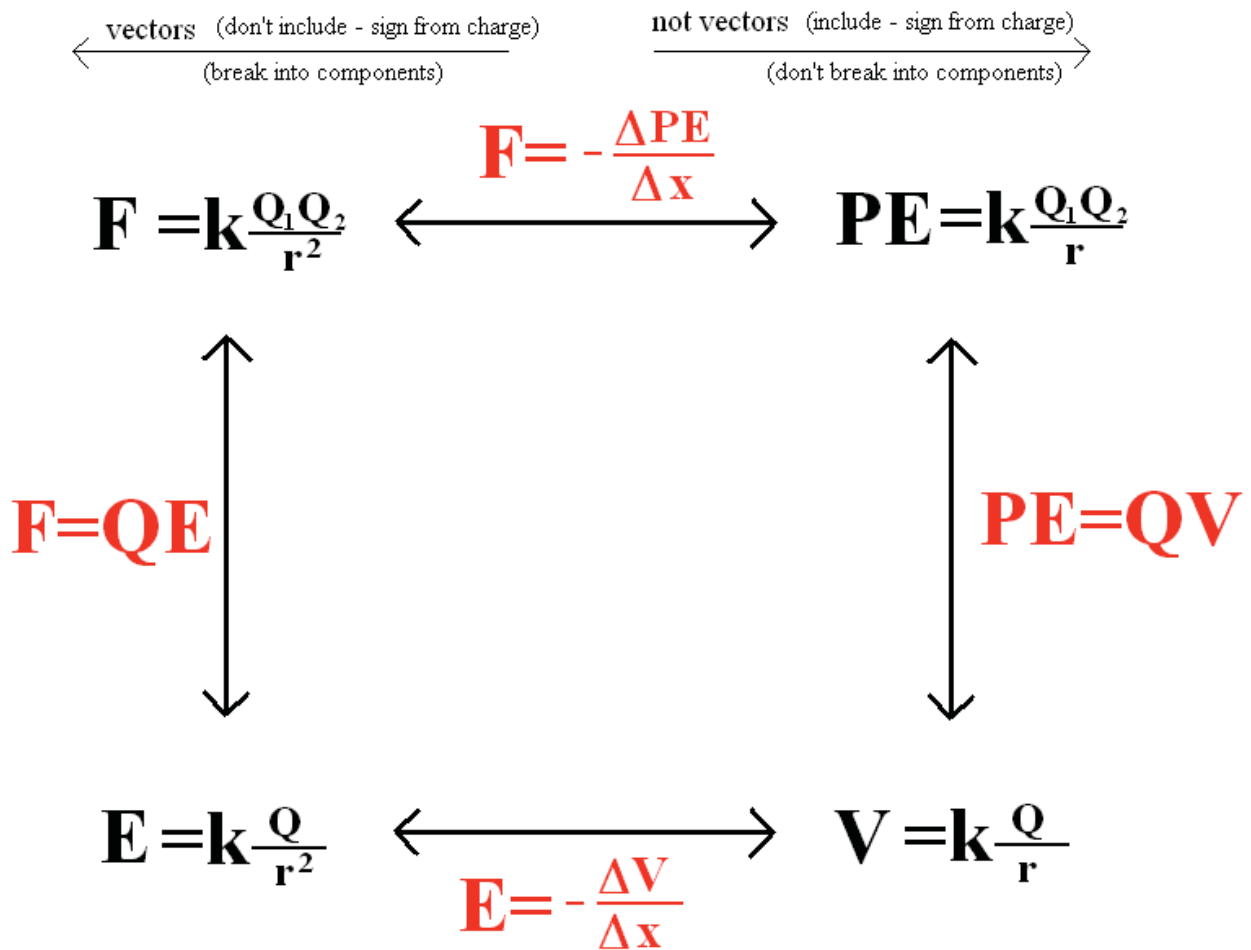
+ charges create electric fields that point radially outward from charge, - charges create E pointing inward

**PE<sub>electric</sub>** is electric potential energy [Joules]

Electric Poetential Energy (PE) is another form of energy that objects can have

**V** is electric potential [J/Coulomb or Volts]

Electric Potential (V) at a point is the Electric Potential Energy (PE) 1C of charge would have at that point



**Note:** + and - charges both feel a force toward lower PE<sub>electric</sub>, also Electric fields E point toward lower V

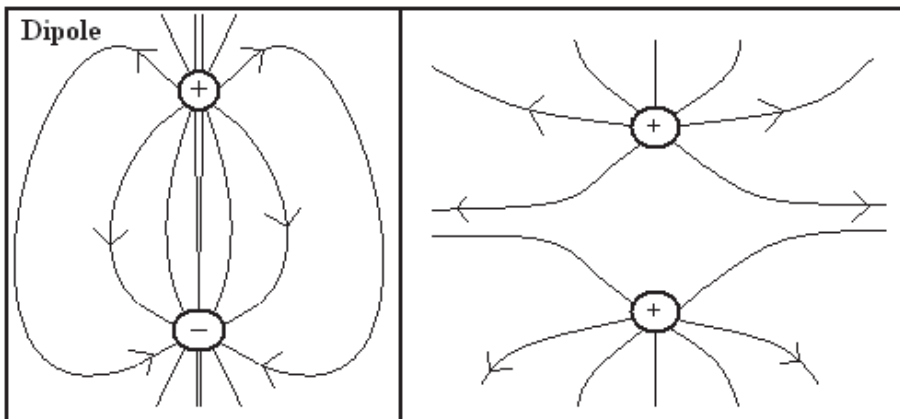
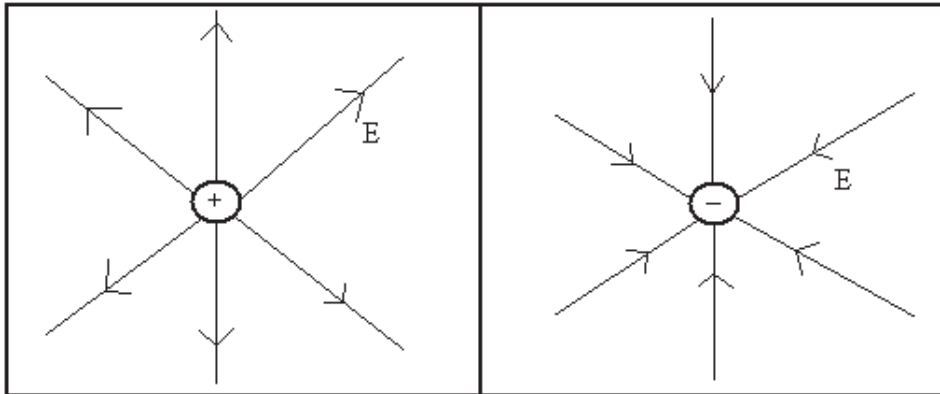
# Electric Field Lines and Equipotential Lines

**Electric Field Lines** show the direction of the electric field ( $E$ ) at points in space.

Field lines point radially outward from “+” charges, and radially inward toward “-” charges.

The Electric field  $E$  is greatest where field lines are closest together.

Larger charges get more field lines to start/end on them.

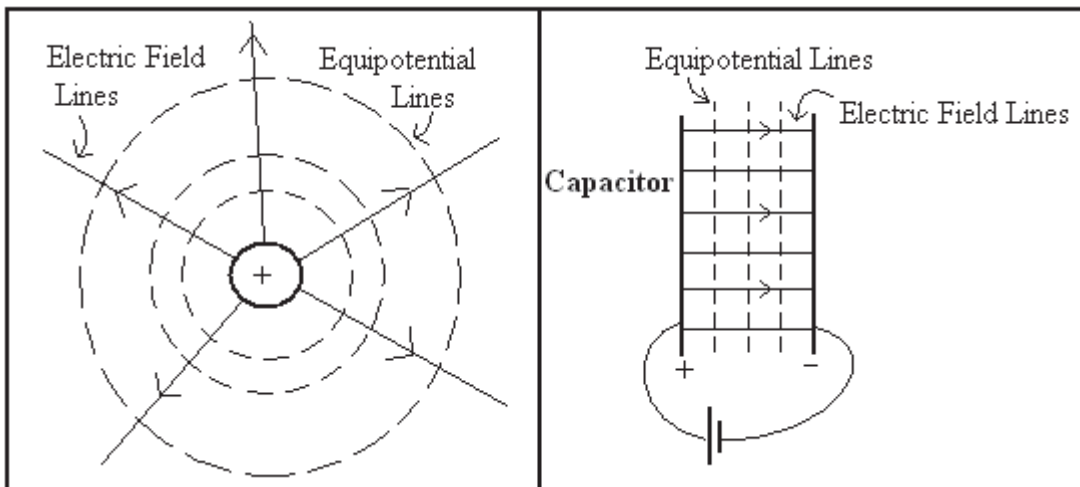


**Equipotential Lines** show lines of constant electric potential ( $V$ ).

Equipotential Lines are always perpendicular to the Electric Field Lines.

The Electric Field  $E$  is greatest where Equipotential Lines are closest together,  $E = -\Delta V / \Delta x$

There is no work done when a charge is moved along an Equipotential Line.



# Circuits

## Current

$$I = Q/t \quad [C/sec = \text{Amperes}]$$

- defined to be in the direction of positive charge flow (or opposite direction of  $e^-$ )
- is directed out of the + terminal of a battery, and into the - terminal

## Resistance

The resistance of a length  $L$  of cylinder made with resistivity  $\rho$ , and cross sectional area  $A$  is,

$$R = \rho L/A \quad [\text{Ohms}]$$

## Ohm's Law

$$V = IR \quad (V \text{ is voltage } \underline{\text{drop across resistor}}, I \text{ is current through the resistor, } R \text{ is resistance)}$$

- $V$  is not necessarily the voltage of the battery!
- **Ohmic materials** have constant resistance (slope on  $V$  vs.  $I$ ), regardless of what the current is
- **Non-Ohmic materials** change their "resistance" depending on what the current/voltage is

## Electrical Power

$$P = IV \quad [\text{Watts}]$$

$$P = I^2R$$

$$P = V^2/R$$

## Capacitors

$$C = Q/V \quad (C \text{ is capacitance, } Q \text{ is charge on + plate, } V \text{ is voltage } \underline{\text{across capacitor}})$$


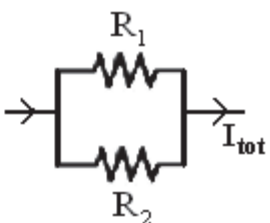
- Capacitance tells you how well a capacitor can store charge
- Inserting a **Dielectric** between a capacitor always **increases capacitance** by a factor of  $k$
- Capacitors store energy as well, which is given by

$$E_{\text{capacitor}} = \frac{1}{2} QV = \frac{1}{2} CV^2$$


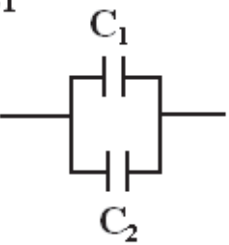
- For a parallel plate capacitor with plates of area  $A$  separated by a distance  $d$ , capacitance is,

$$C = \epsilon_0 A/d$$

## Combining Resistors

<p>Resistors in Series</p> $R_{eq} = R_1 + R_2$  <p>Note: Resistors in Series always have same current</p>	<p>Resistors in Parallel</p> $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$  <p>Note: Resistors in Parallel always have same voltage</p>
<p><b>If circuit has only 1 battery,</b> Choose resistors, two at a time, and reduce to a single resistor to determine the current through the battery. Then determine how current breaks up at junctions using these rules</p>	<p>If one resistor is 3 times larger than the other, smaller resistor gets 3/4 of the total current <math>I_{R_1} = \frac{3}{4} I_{tot}</math></p> <p>If one resistor is 5 times larger than the other, smaller resistor gets 5/6 the total current <math>I_{R_1} = \frac{5}{6} I_{tot}</math></p> <p>or, if resistors are not a nice ratio use this formula</p> $I_{R_1} = I_{tot} \frac{R_2}{(R_1 + R_2)}$

## Combining Capacitors

<p>Capacitors in Series</p> $\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$  <p>Note: Capacitors in series all have same charge</p>	<p>Capacitors in Parallel</p> $C_{eq} = C_1 + C_2$  <p>Note: Capacitors in parallel all have same voltage</p>
<p>When you reduce all capacitors to a single C, you can find Q (=CV). Then work backwards to find Q on each capacitor.</p>	<p>For capacitors in parallel, if one capacitor has 3 times more capacitance than the other, it gets 3/4 of the total charge.</p> <p>Or, if not a nice ratio use,</p> $Q_1 = Q_{tot} \frac{C_1}{C_1 + C_2}$
<p>Note: After a short time, current will no longer flow through a C, and any segment of a circuit with a C will have no current.</p>	

## Kirchoff's Rules

### Junction Rule: $I_{in} = I_{out}$

- Total current flowing into junction equals total current flowing out of junction

### Loop Rule: $\Sigma \Delta V = 0$

- The sum of the changes in voltage around any closed loop always equals zero

$\Delta V = -IR$  (if you **pass through** resistor in the **same direction as current**)

$\Delta V = IR$  (if you **pass through** resistor in the **opp. direction as current**)

$\Delta V = +\epsilon_{battery}$  (if you **pass through** the battery from **- terminal to + terminal**)

$\Delta V = -\epsilon_{battery}$  (if you **pass through** the battery from **+ terminal to - terminal**)

## Terminal Voltage

$V_{ab} = \epsilon - Ir$  ( $v_{ab}$  is the terminal voltage,  $\epsilon$  is the emf of battery,  $r$  is internal resistance)

- Every battery has an internal resistance  $r$  which will lower the terminal voltage when current flows

- A 9V battery will not necessarily have a measured terminal voltage of 9V, unless no current flows

- The  $\epsilon$  of a 9V battery is 9V even when no current flows, but the measured terminal voltage will be less

- **Slope** of  $V_{ab}$  vs.  $I$  graph is negative the **internal resistance**. The **y intercept** is the **emf  $\epsilon$** .

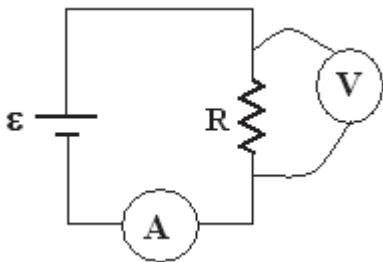
## Electrical Meters

### Voltmeter

- Measures voltage change across circuit element (resistor, battery, etc.)

- Ideally has **infinite resistance** so it does not draw any current away from circuit

- Needs to be hooked up in **parallel** with circuit element



### Ammeter

- Measures current through a circuit element (resistor, battery, etc.)

- Ideally has **no resistance** so it does not change the current

- Needs to be hooked up in **series** with circuit element



# Magnetism

## Magnetic forces

$$\mathbf{F}_B = q\mathbf{v}B\sin\theta \quad (\mathbf{q} \text{ is charge, } \mathbf{v} \text{ is speed, } \mathbf{B} \text{ is magnetic field, } \theta \text{ is angle between } \mathbf{v} \text{ and } \mathbf{B})$$

- The direction of force on + charge is given by the **Right hand rule** (Very-Bad-Finger)
- If the charge is negative the force is in the opposite direction
- Magnetic forces **never do Work** (since  $F_B$  is always **perpendicular** to motion  $W = Fd\cos 90 = 0$ )
- Magnetic forces often make charges ( $q$ ) of mass  $m$  travel in circles of radius  $r$  given by,

$$r = mv/qB$$

Note: If you want a charged particle to travel in a **straight line ("velocity selector")**, create an electric field  $E$  so that the forces cancel, i.e. speed is ratio of  $E$  to  $B$

$$\mathbf{v} = \mathbf{E}/\mathbf{B} \quad (\text{since } F_B = F_E \text{ or } qvB = qE)$$

Note: The forces have to be of equal size, not the fields! (i.e.  $F_B = F_E$ , but  $E$  does not equal  $B$ )

## Magnetic force on wire

$$\mathbf{F}_B = \mathbf{ILB} \quad (\mathbf{I} \text{ is current that feels force, } \mathbf{L} \text{ is length of wire, } \mathbf{B} \text{ is mag. field from other sources)}$$

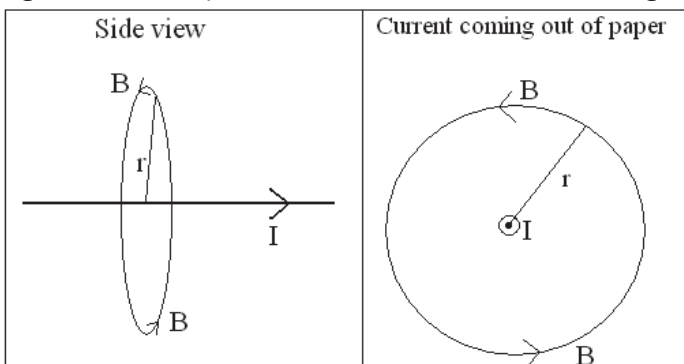
-to find direction of  $F_B$  use the same right hand rule (except  $v$  is now direction of  $I$ )

## Magnetic fields

The magnetic field a distance  $r$  from a long straight current ( $I$ ) carrying wire is given by,

$$\mathbf{B} = \mu_0 I / 2\pi r \quad [\text{Tesla}] \quad \mu_0 = 4\pi \times 10^{-7} \text{ T m/A}$$

- The magnetic field from a long straight wire is directed along a circle centered at wire with direction given by right hand rule (Thumb in direction of current, fingers curl in direction of  $B$ )



- Note: Wires with  $I$  in same direction will attract, Wires with  $I$  in opp. Direction will repel

## Induced voltage $\mathcal{E}$

$$\mathcal{E} = - \Delta \Phi_M / \Delta t \quad (\text{magnetic flux } \Phi_M = BA \cos \theta \quad A \text{ is the area of the loop of wire})$$

$$\mathcal{E} = \Delta(BA \cos \theta) / \Delta t$$

- You will induce a voltage in a loop of wire if you change **B**, **A**, or  **$\theta$**

For a piece of wire or a conducting bar of length **L** the induced voltage will be

$$\mathcal{E} = LvB \quad (\text{remember there is voltage on Las Vegas Boulevard})$$

## Lenz's Law

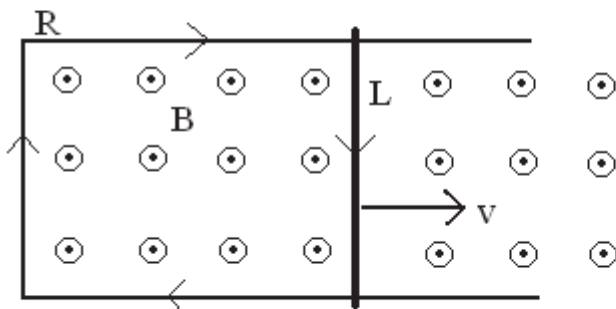
- Induced current always opposes the change in flux

If flux increases, induced current creates a magnetic field **B** in opp direction of existing **B**

If flux decreases, induced current creates a magnetic field **B** in same direction of existing **B**

Ex 1:

**flux increases** so induced magnetic field goes  
in opposite direction of existing **B** field  
(put thumb into paper to get CW current)



$$F = ILB$$

$$F = (\mathcal{E}/R) L B$$

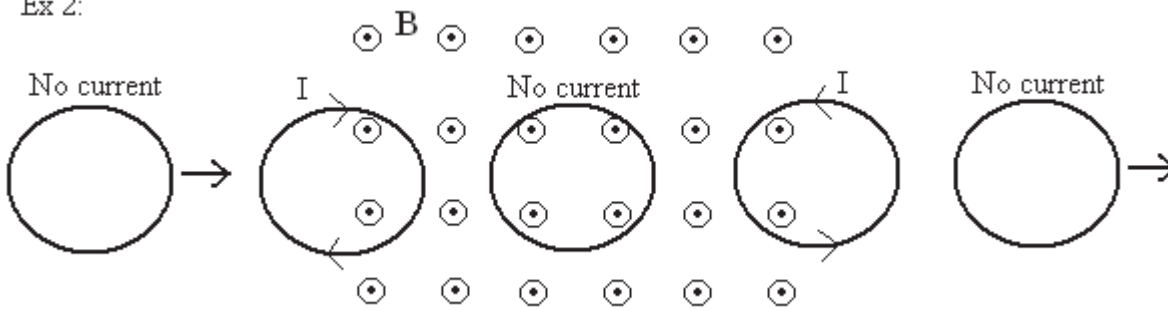
$$F = (LvB/R) L B$$

$$F = L^2 B^2 v / R$$

Induced **I** goes CW  
to create **B** into paper

$$P = Fv \text{ or } IV$$

Ex 2:



# Optics

**Reflection**  $\theta_{in} = \theta_{out}$

Note: always measure  $\theta$  from the normal line

**Refraction**  $n_1 \sin \theta_1 = n_2 \sin \theta_2$

$$n = c/v = (3 \times 10^8 \text{ m/s})/v$$

Index of refraction  $n$  is always greater than or equal to 1

When a wave passes from a **fast medium to a slow medium** it bends **"toward the normal"**

When a wave passes from a **slow medium to a fast medium** it bends **"away from the normal"**

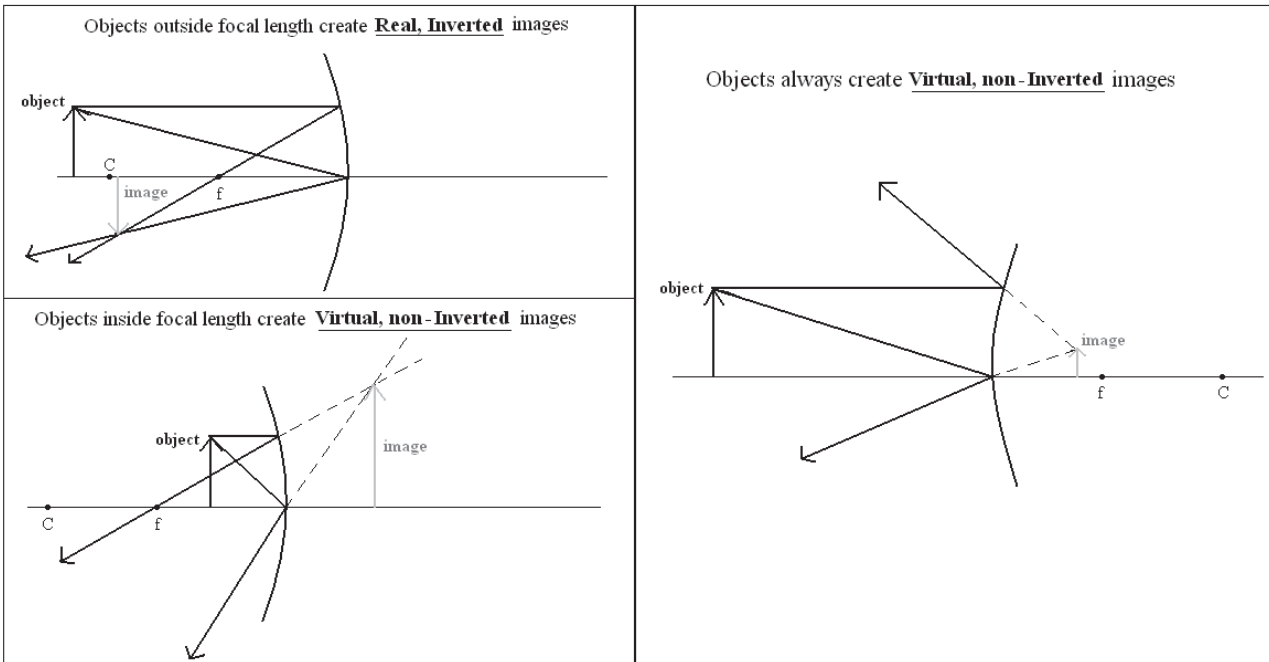
Total internal reflection:  $\sin \theta_{critical} = n_2/n_1$  (Note: TIR only occurs if reflected off of "fast" medium)

## Ray tracing for Mirrors

(one ray parallel, and one ray into the center)

Concave Mirror

Convex Mirror

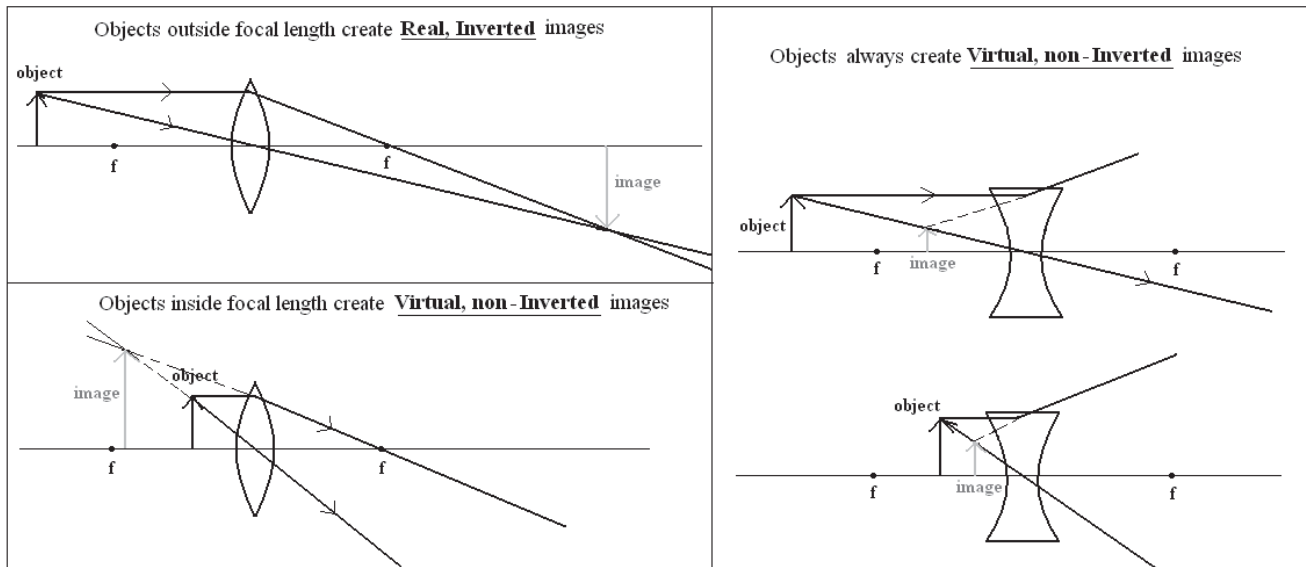


## Ray tracing for Lenses

(one ray parallel, and one ray into the center)

Convex lens (Converging lens)

Concave lens (Diverging lens)



# Mirror or Lens Equation

# Magnification equation

$$1/f = 1/d_o + 1/d_i$$

$$M = h_i/h_o = - d_i/d_o$$

## Things that are true for all mirrors/lenses

$d_i$  is + if image is closer to you than mirror/lens

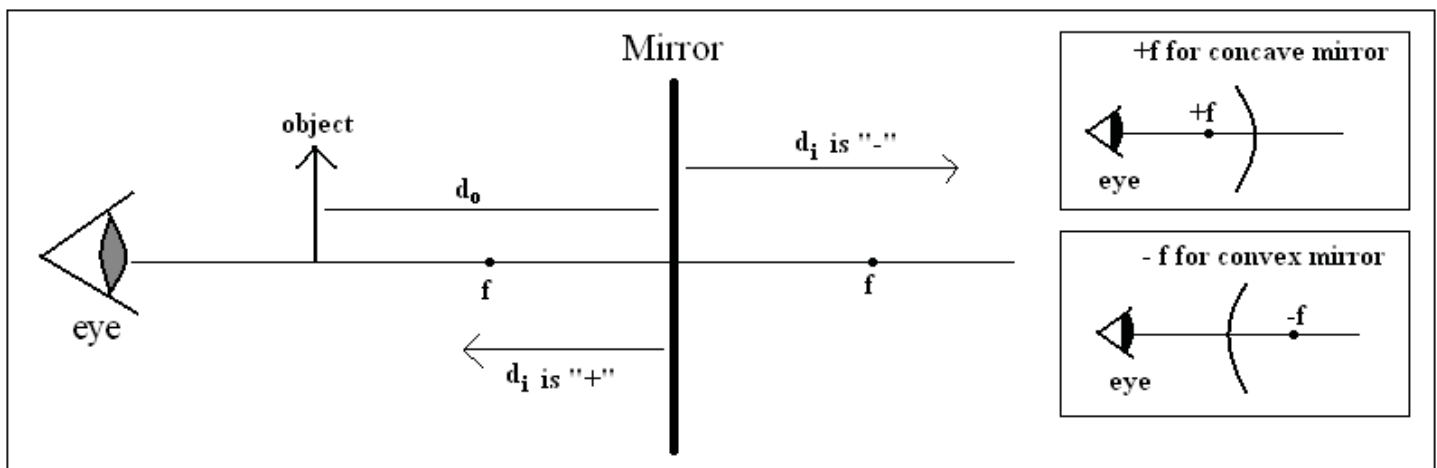
$d_i$  is - if image is farther from you than mirror/lens

**Virtual Image**  
 $d_i$  is "-"  
Right side up

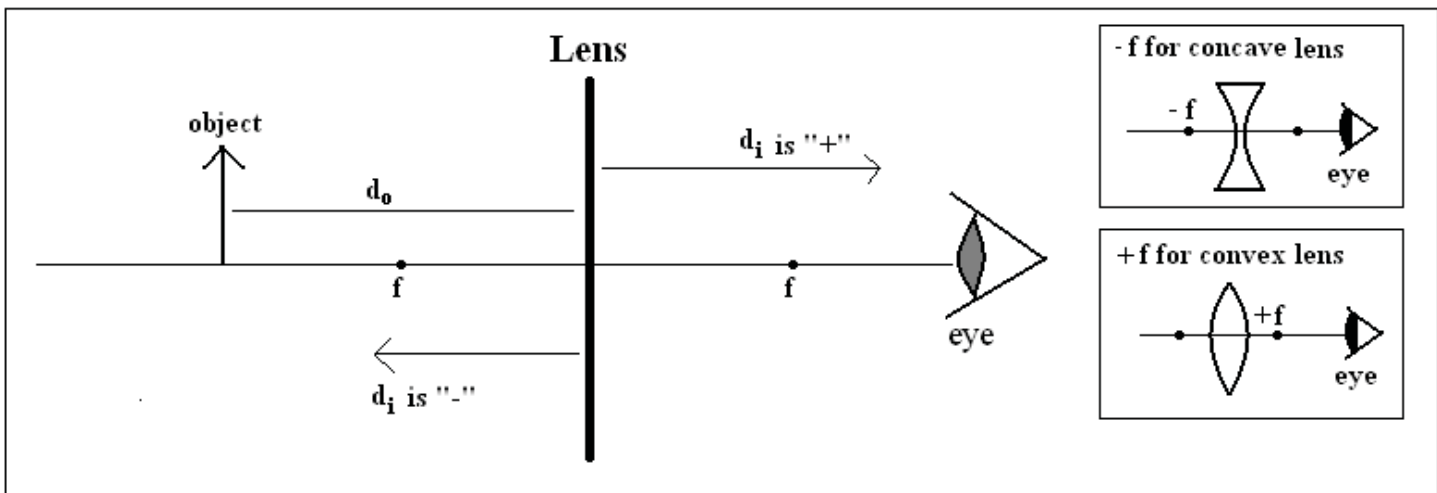
← ————— →  
These always go together  
(if one is true, the others are true)

**Real Image**  
 $d_i$  is "+"  
Upside down

## For Mirrors



## For Lenses



## Wave phenomenon

**Reflection**  $\theta_{in} = \theta_{out}$

Note: always measure  $\theta$  from the normal line

**Refraction**  $n_1 \sin \theta_1 = n_2 \sin \theta_2$

$$n = c/v = (3 \times 10^8 \text{ m/s})/v$$

Index of refraction  $n$  is always greater than 1

When a wave passes from a **fast medium to a slow medium** it bends **"toward the normal"**

When a wave passes from a **slow medium to a fast medium** it bends **"away from the normal"**

Total internal reflection:  $\sin \theta_{critical} = n_2/n_1$  (Note: TIR only occurs if reflected off of "fast" medium)

**Diffraction:** The spreading out of waves when they encounter a hole or corner

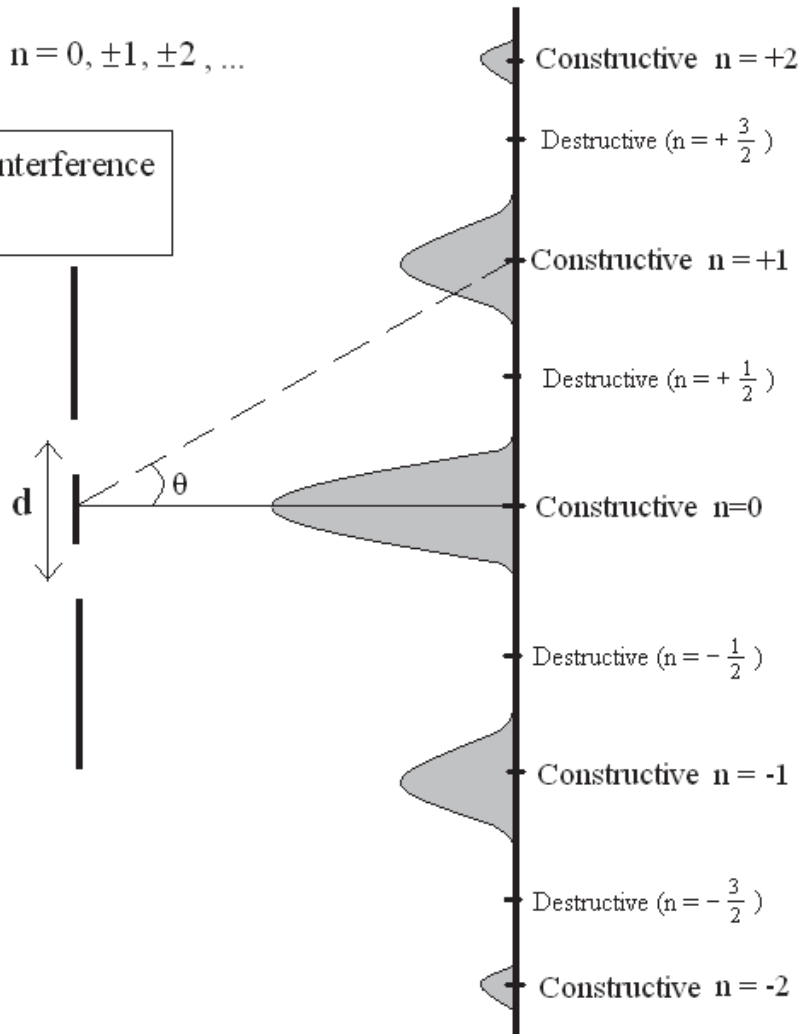
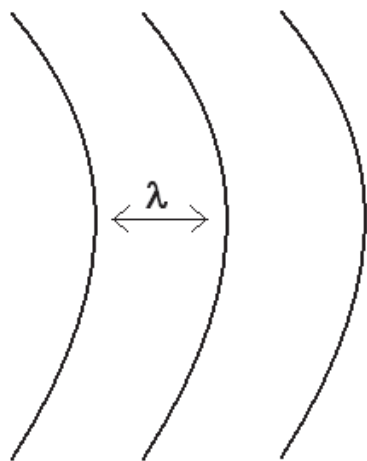
## Double Slit Diffraction

Constructive  
Interference

$$n \lambda = d \sin \theta$$

$$n = 0, \pm 1, \pm 2, \dots$$

Note: To find the angles of Destructive Interference  
just plug in  $n = \pm \frac{1}{2}, \pm \frac{3}{2}$  etc



**For Single Slit Diffraction**, it is the opposite,

i.e. **Destructive** happens for  $n\lambda = d \sin \theta$   $n = \pm 1, \pm 2, \pm 3$  (don't use  $n=0$  here!)

# Thin film interference

For **Fast -> Slow -> Fast** interference (e.g. a soap bubble, or a thin piece of plastic)

**Fast → Slow → Fast**

Constructive Interference →  $2t = (m + \frac{1}{2}) \frac{\lambda}{n}$

Dest. Interference →  $2t = m \frac{\lambda}{n}$

**t** is the thickness of the Thin film

**n** is the index of refraction of the Thin film

$\lambda$  is the wavelength of the light in the air

**m** = 0, 1, 2, ...

air (fast)

Thin film (slow)  
index of refraction **n**

air (fast)

Note: Wavelength of the light in thin film is  $\frac{\lambda}{n}$

For **Fast -> Slow -> Slower** interference (e.g. water on glass)

**Fast → Slow → Slower**

Constructive Interference →  $2t = m \frac{\lambda}{n}$

Dest. Interference →  $2t = (m + \frac{1}{2}) \frac{\lambda}{n}$

**t** is the thickness of the Thin film

**n** is the index of refraction of the Thin film

$\lambda$  is the wavelength of the light in the air

**m** = 0, 1, 2, ...

air (fast)

Thin film (slow)  
index of refraction **n**

Slower medium than Thin film (slower)

Note: Wavelength of the light in thin film is  $\frac{\lambda}{n}$

# Modern Physics

## Photons

$$E = hf \quad (\text{f is frequency, h is Planck's constant } h = 6.626 \times 10^{-34} \text{ J sec})$$

$$\lambda = h/p \quad (\text{p is momentum, } \lambda \text{ is wavelength})$$

- Higher frequency (lower wavelength) light has more energy per photon

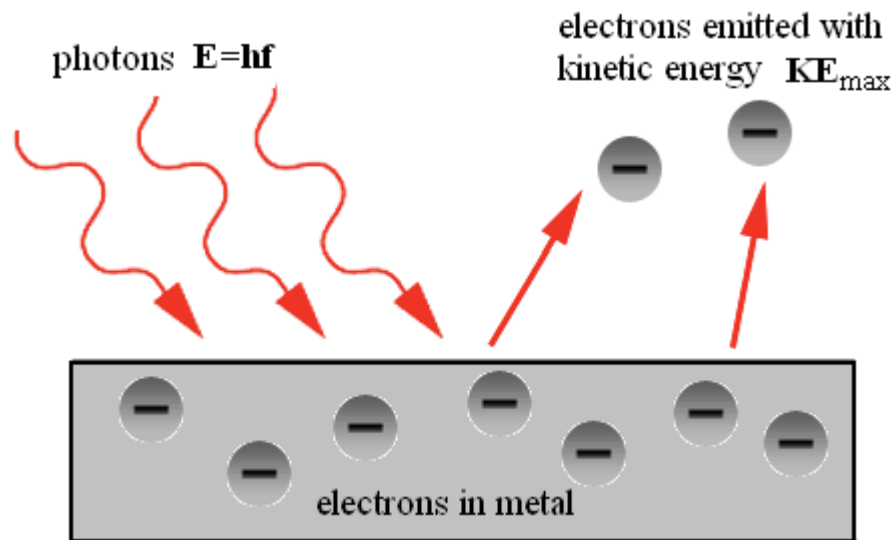
- 1 eV (electron Volt) =  $1.6 \times 10^{-19}$  Joules

- Note:  $\lambda = h/p = h/mv$  works for electrons and other particles too. (DeBroglie Wavelength)

## Photoelectric Effect

- Provided evidence that light behaves like a particle (photon)

$$KE_{\max} = hf - \phi \quad (\phi \text{ is the work function. Energy needed to free electron from metal.})$$



- Increasing Intensity of light (number of photons) increases number of electrons

- Increasing frequency of light (energy of photons) increases  $KE_{\max}$  of electrons

$$\text{Stopping potential: } \Delta V = KE_{\max}/e$$

- Stopping potential is the minimum voltage needed to stop the outgoing electrons

## Compton Scattering

- Photons collide and scatter off other particles (typically electrons)

- Provided more evidence that light behaves like a particle, since photons collide like particles

- Wavelength of scattered light always increases by an amount,

$$\lambda - \lambda_0 = h/m_e c (1 - \cos\theta) \quad (\theta \text{ is the angle between scattered and incident photons})$$

- The photon always decreases in energy, decreases in frequency, and increases in wavelength

## Nuclear processes

A  
Z X

X is the element name (H for Hydrogen or Pb for Lead)

mass number A is the total # of nucleons (protons + neutrons)

atomic number Z is the # of protons

neutron number N is A - Z (number of neutrons)

**Alpha Decay** e.g.  ${}^{238}_{92}\text{U} \rightarrow {}^{234}_{90}\text{Th} + {}^4_2\text{He}$

- An alpha particle, i.e. a Helium nucleus (2 protons + 2 neutrons), is emitted by a larger nucleus
- mass number **A decreases by 4** and atomic number **Z decreases by 2**

**Beta Decay** e.g.  ${}^{14}_6\text{C} \rightarrow {}^{14}_7\text{N} + e^- + \text{antineutrino}$

- Typically a neutron decays into a proton, electron and antineutrino
- mass number **A always stays the same**
- atomic number **Z typically increases by 1** (if neutron decays into proton)
- Occasionally a proton can absorb an electron and turn into a neutron. In this case Z decreases by 1

**Gamma Decay** e.g.  ${}^{12}_6\text{C}^* \rightarrow {}^{12}_6\text{C} + \gamma$  (X\* denotes an excited nucleus)

- A high energy photon (Gamma ray) is emitted by an excited nucleus
- Mass number **A and atomic number Z remain the same**
- Gamma decay typically occurs after an alpha or beta decay

**Mass Defect** (The total mass often changes in nuclear reactions like fission and fusion)

$$E_{\text{rest energy}} = mc^2 \quad \text{or} \quad \Delta E = \Delta mc^2$$

- Mass can be converted into energy ( $e^- + e^+ \rightarrow \gamma$ 's), and energy can be converted into mass

**Atomic energy levels** ( $e^-$  emit photons if drop E levels, absorb photons if rise E levels)  
electron energy levels in an atom

