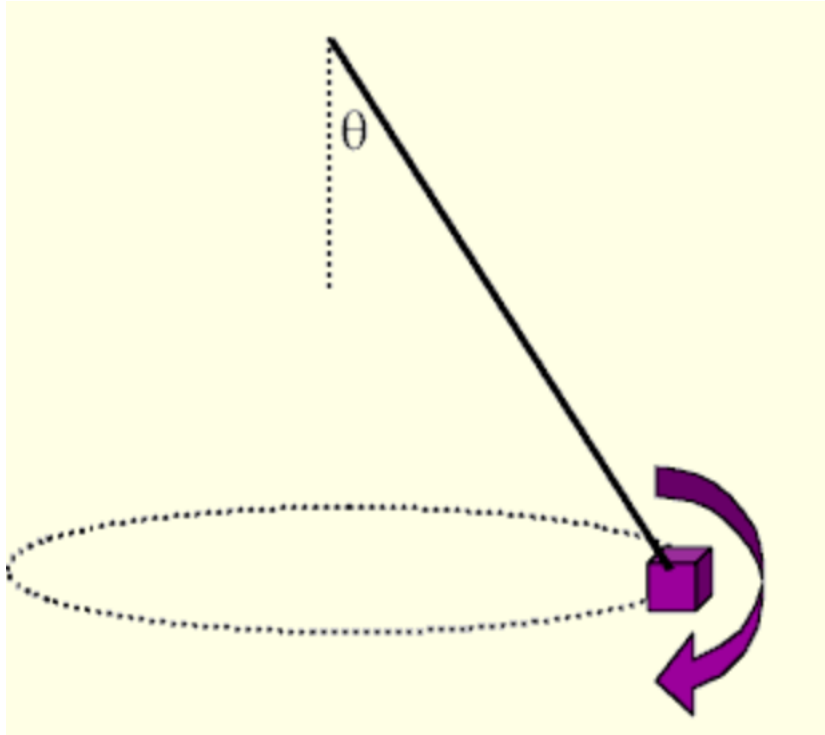
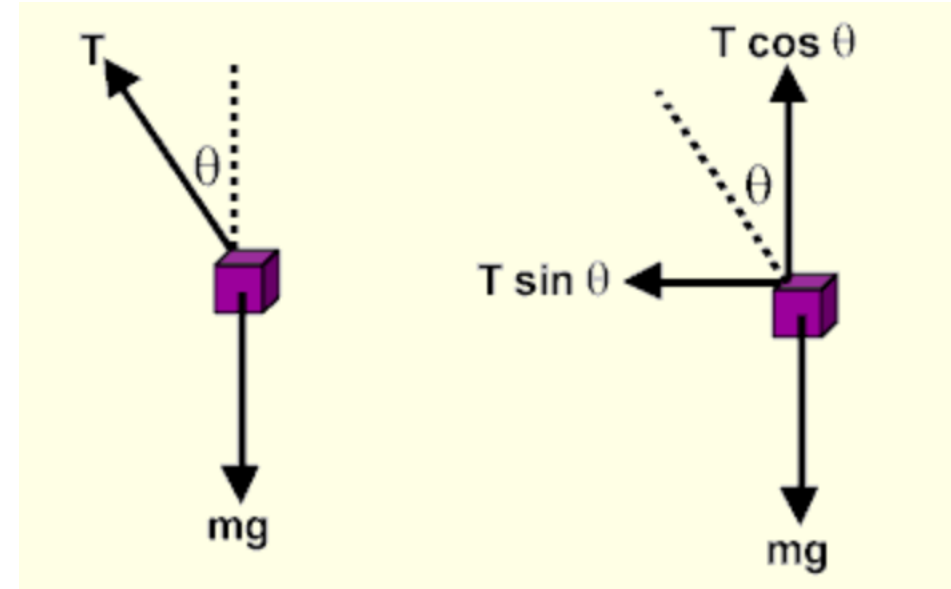


UNIFORM CIRCULAR MOTION WITH TENSION

Images are from the lesson resources at physicslab.org; <http://dev.physicslab.org/Lessons.aspx>



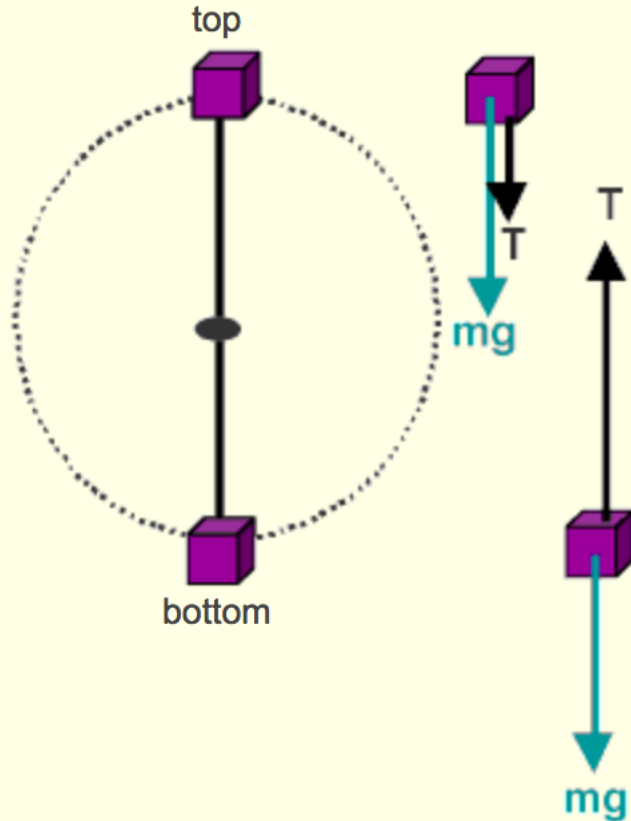
Object path is in the horizontal plane;
Everywhere on the path, the net force is
the same.



Since $T \cos \theta = mg$, the centripetal force (the net force) is $T \sin \theta$

NON-UNIFORM CIRCULAR MOTION WITH TENSION

Images are from the lesson resources at physicslab.org; <http://dev.physicslab.org/Lessons.aspx>



When the tension in the rope approaches zero...

$$\begin{aligned}0 &= m(v^2/r) - mg \\m(v^2/r) &= mg \\v^2/r &= g \\v^2 &= rg \\v &= \sqrt{rg}\end{aligned}$$

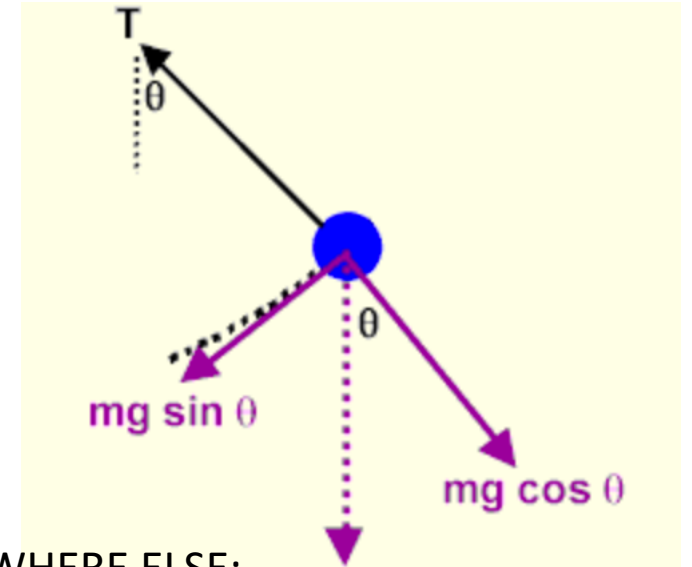
...the minimum speed needed to get around the top of the circle can be found

TOP:

$$\begin{aligned}\text{net force to the center} &= T + mg \\F_c &= T + mg \\m(v^2/r) &= T + mg \\T &= m(v^2/r) - mg\end{aligned}$$

BOTTOM:

$$\begin{aligned}\text{net force to the center} &= T - mg \\F_c &= T - mg \\m(v^2/r) &= T - mg \\T &= m(v^2/r) + mg\end{aligned}$$



EVERYWHERE ELSE:

$$\begin{aligned}\text{net } F_c &= T - mg \cos \theta \\mv^2/r &= T - mg \cos \theta \\T &= mv^2/r + mg \cos \theta\end{aligned}$$